

Solution Sheet on Problem Set 4

**Fixed Income**

Deadline: 16.12.2021

**Solved by: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_**

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| **Task** |  | **Points Earned** |
| 1. **Forwards to Interest**   a)  Different types of interest rates  (9 points) |  |  |
| b)  Z-Bond prices  (7 points) |  |  |
| c)  Forward Rate (3y to 20y) (4 points) |  |  |
| 1. **Fix.Inc. Calculus**   a)  Coupon bond price (4 points) |  |  |
| b) Yield-to-maturity  (4 points) |  |  |
| c) Bond Duration’s  (6 points) |  |  |
| d) Scenarios: description (6 points) |  |  |
| e) Scenarios: YTM (10 points) |  |  |
| f) Scenarios: prices (10 points) |  |  |
| **3. Yield Curve** a) Yield curve patterns (4 points) |  |  |
| b)  Z-bond prices (6 points) |  |  |
| c) Yield curve fit (8 points) | **For the below regression:**  **x1 = m, i.e. the tenor**  **x2 = m^2, i.e. the tenor squared**  **x3 = m^3, i.e. the tenor cubed**  **A screenshot of a computer  Description automatically generated with medium confidence**  **Adding the fitted line to the chart from 3b)**  **Chart, line chart  Description automatically generated** |  |
| d) 7 year z-bond (5 points) | Value of a 7y Zero Coupon Bond: 103.39362 (assuming Face value = 100) |  |
| e) Semi-annual coupon bond (5 points) | Value of a 3y semi annual Coupon Bond: 105.32263 |  |
| f) Level, slope & curvature (6 points) | # level = y10  # slope = y10 -y3m  # curvature = (y2-y3m) - (y10 - y2)  It can be observed that the level (i.e. the 10y interest rate) steadily decreases from roughly 4% to below 0%.  Between 2000 and 2004 an increase in the slope can be seen. Given that we don’t see the same corresponding increase of the 10y rate a decrease in the 3month rate is implied. It can be theorized that this is a direct consequence of the dot com bubble. At the same time a decrease in curvature is examined. Due to the increase in the slope and the decrease in curvature it can be inferred that the 3 months rate dropped more relatively to the 2y and 10y rates.  Another very large move of the slope as well as curvature can been seen shortly after 2008 (financial crisis). The sharp increase in the slope must be from a sharp decrease in the 3 months rate, because we don’t observe a very large move in the level (10y rate). To soften the impact of the financial crisis the Central Bank decreased interest rates on the short end.  Interestingly, for the Covid crisis which started in March 2020 we do not see such large changes in level, slope, and curvature. One potential explanation for this could be that the Central Bank was already effectively at the zero lower bound at that point in time and from a rates perspective did not have much room to react to the crisis. Instead, the Central Bank had to resort to other measures such as other methods such as enormous asset purchase programs (e.g. PEPP for the ECB).  **Chart, line chart, histogram  Description automatically generated** |  |
| g) Different Spreads (6 points) | The plot below displays the spread of 10y AA corps as well as BBB corps over the 10y Government Rate. This can also be referred to as the risk premium, as generally the assumption is that the government risk in the respective currency is the risk free rate for this tenor. Clearly, the risk premium for the AA rated corps is lower than the BBB rated corps, which are barely IG rated (anything below BBB- is considered high yield). In addition to the higher risk premium, the lower rated corps also have a higher volatility. For both the AA and BBB corps an increase in risk premium can be observed at the start of the Covid crisis in March 2020, which subsequently recovered fairly fast – this is partly because of the central banks (e.g. Fed, ECB, SNB) that bought these bonds in the aftermath of the Covid crisis to ensure that the bond market remains sufficiently liquid and that companies could refinance themselves at cheap levels. **Chart, line chart  Description automatically generated** |  |